### Method for Development of Probabilistic Emission Inventories: Example Case Study for Utility NO<sub>x</sub> Emissions

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### **Objectives**

- Demonstrate a general probabilistic approach for quantification of variability and uncertainty in emission factors and emission inventories
- Demonstrate identification of key sources of uncertainty in an inventory in order to target future work to improve the inventory
- Develop a prototype software tool for calculation of variability and uncertainty in statewide inventories for a selected emission source and pollutant

### Introduction

- Emission Inventories (Els) are a vital component of environmental decision making.
- Characterize and evaluate the quality of emission inventories.
- Quantitative approach to characterizing both variability and uncertainty.
- Case study of NO<sub>x</sub> emissions from electric utility power plants.
- A prototype software tool was developed to convey the example.

### **General Methodological Approach**

- Compilation and evaluation of database
- Visualization of data by developing empirical cumulative distribution functions
- Fitting, evaluation, and selection of alternative parametric probability distribution models
- Characterization of uncertainty in the distributions for variability
- Propagation of uncertainty and variability in activity and emissions factors to estimate uncertainty in total emissions
- Calculation of importance of uncertainty

### **Compilation and Evaluation of Database**

- Preliminary Summary Emissions Reports
  - –Acid Rain Program of the U.S. EPA (http://www.epa.gov/acidrain/etsdata.html)
  - -Quarterly Values Report
- Data Combination (Multiple Quarters)
- Data Screening
- Calculation of Emission Factors and Activity Factors for 6-month and 12-month averages
- Setup of the Internal Database for the prototype software tool

### Fitting, Evaluation and Selection of Probability Distribution Models

- Distribution types
  - Normal

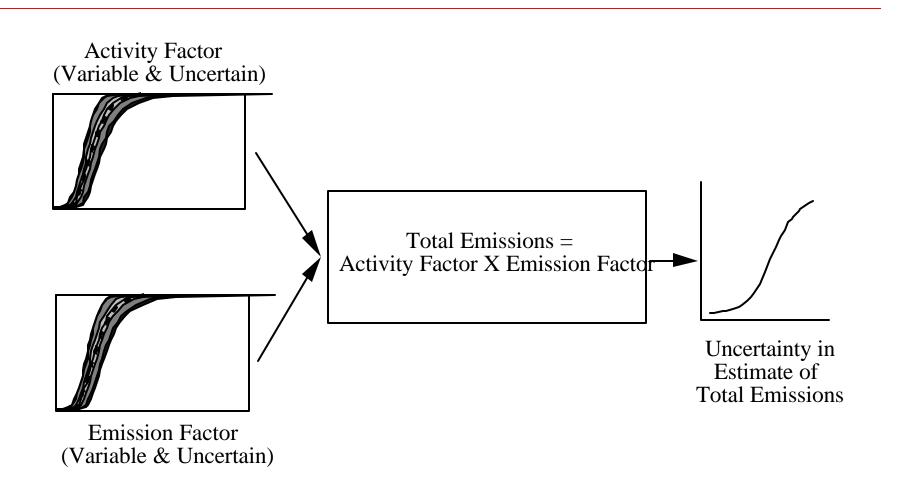
- Lognormal

Gamma

- Weibull

- Beta
- Parameter estimation methods
  - Method of Matching Moments (MoMM)
  - Maximum Likelihood Estimation (MLE)
- Evaluation of goodness of fit
  - Statistical tests
  - Subjective judgment by visualization of data and fit
- Bootstrap simulation used to quantify uncertainty

### **Probabilistic Emission Inventories**



### **Emission Inventory Model**

 Emission Inventory Model based on electric utility power plants:

$$E = EF \bullet HR \bullet CP \bullet C$$

### Where:

E = emissions (e.g., lb of NO<sub>x</sub> as NO<sub>2</sub>)

EF = emission factor (e.g., lb of NO<sub>x</sub> as NO<sub>2</sub> per ton of coal burned)

HR= heat rate (BTU/kWh)

CP = capacity factor

C = capacity load (MW)

## Identification of Key Sources of Uncertainty

- Importance of Uncertainty
  - Multi-linear Regression
  - Correlation Coefficient
  - Probabilistic Sensitivity Analysis
- Correlation coefficient was chose in the prototype software tool  $\sum_{k=1}^{m} (x_k \overline{x})(y_k \overline{y})$

$$U_{\rho} = \frac{\sum_{k=1}^{m} (x_{k} - \overline{x})(y_{k} - \overline{y})}{\sqrt{\sum_{k=1}^{m} (x_{k} - \overline{x})^{2} \times \sum_{k=1}^{m} (y_{k} - \overline{y})^{2}}}$$

 $U_{\scriptscriptstyle D}$ : Importance of uncertainty from model input y samples

 $x_k$ : Model output samples

 $\overline{\chi}$ : The mean of  $x_k$  samples

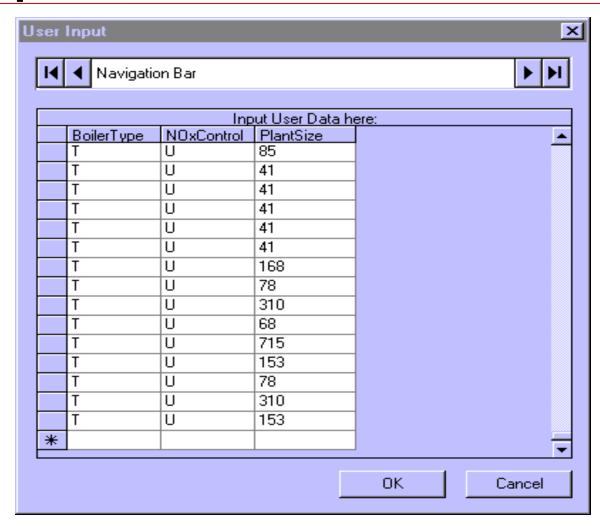
 $y_k$ : Model input samples

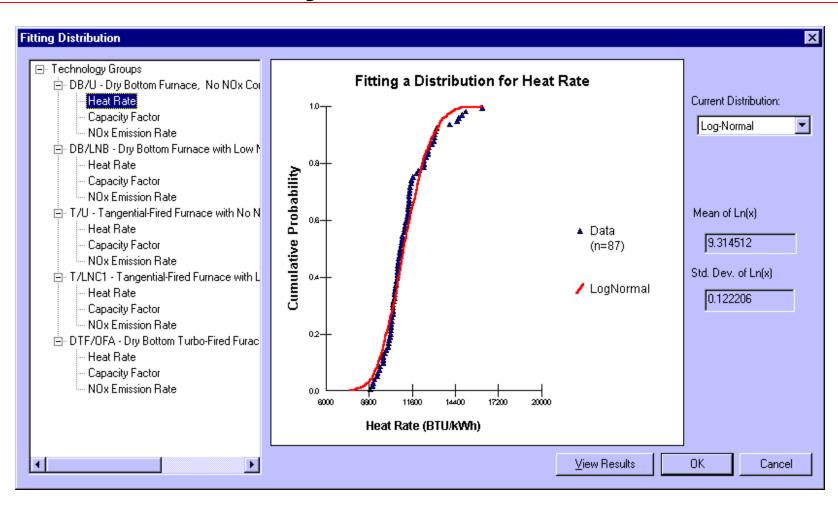
 $\overline{y}$ : The mean of  $y_k$  samples

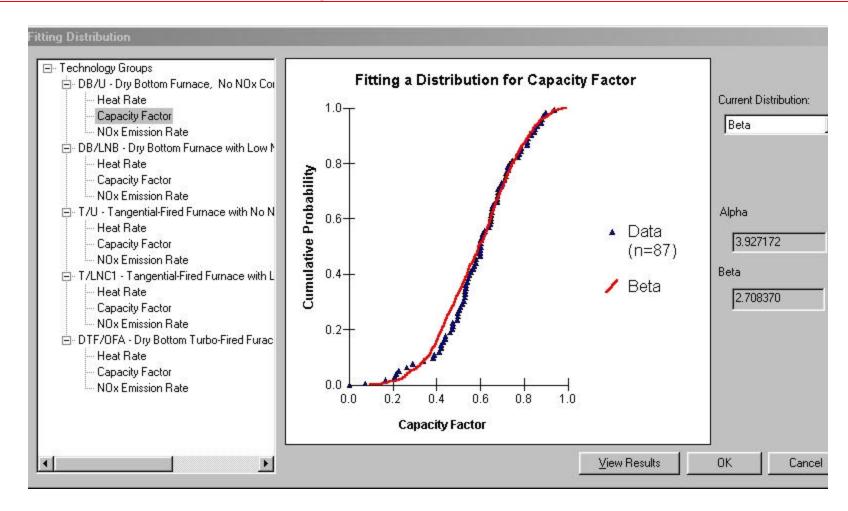
### **Case Study**

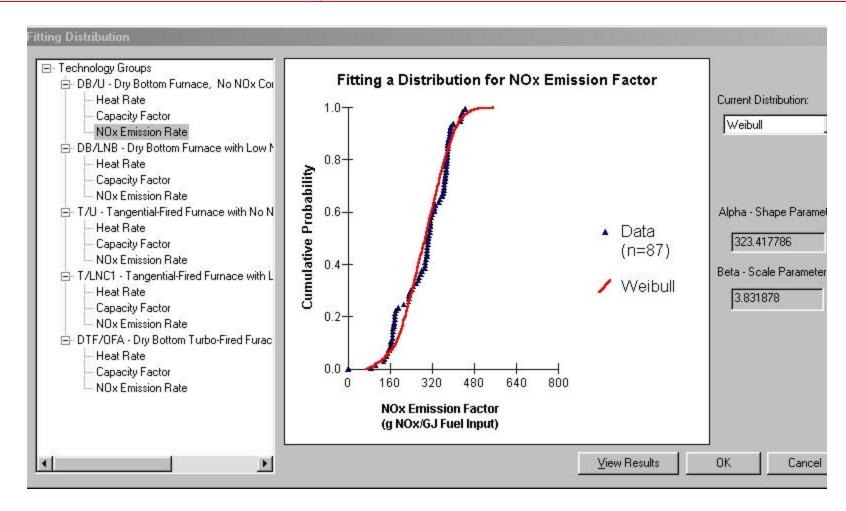
- Power Plant NO<sub>x</sub> Emissions for Selected Power Plants in the State of North Carolina
  - •19 tangential-fired boilers with no  $NO_x$  controls (T/U)
  - •11 tangential-fired boilers using Low NOx Burners and overfire air option 1(T/LNC1)
  - •12 dry bottom wall-fired boilers with no NO<sub>x</sub> controls (DB/U)
  - •3 dry bottom wall-fired boilers using low NO<sub>x</sub> burners (DB/LNB)
- Case study was done using a prototype software tool based on a 6-month average database

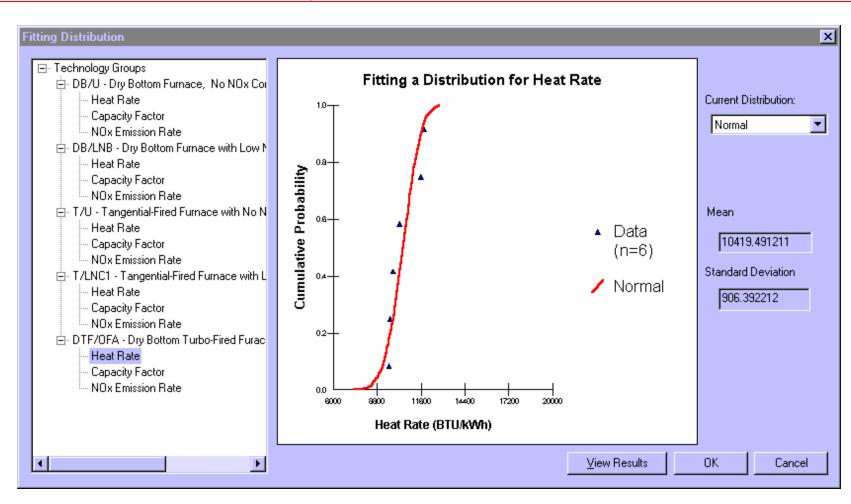
### User Input: Boilier Type, NO<sub>x</sub> Control Option, and Size of Each Unit

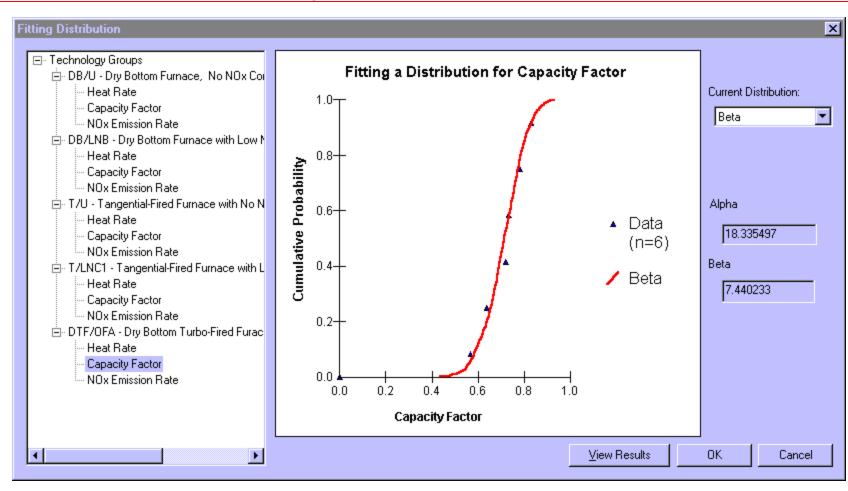


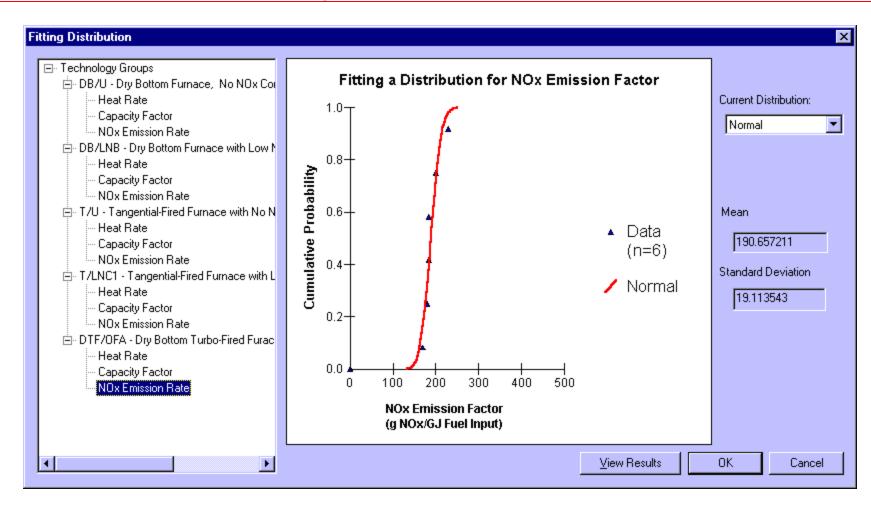




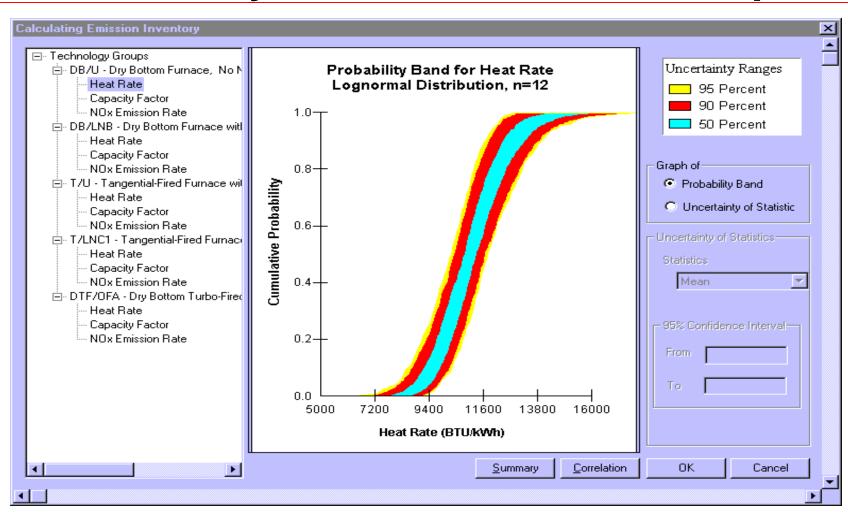




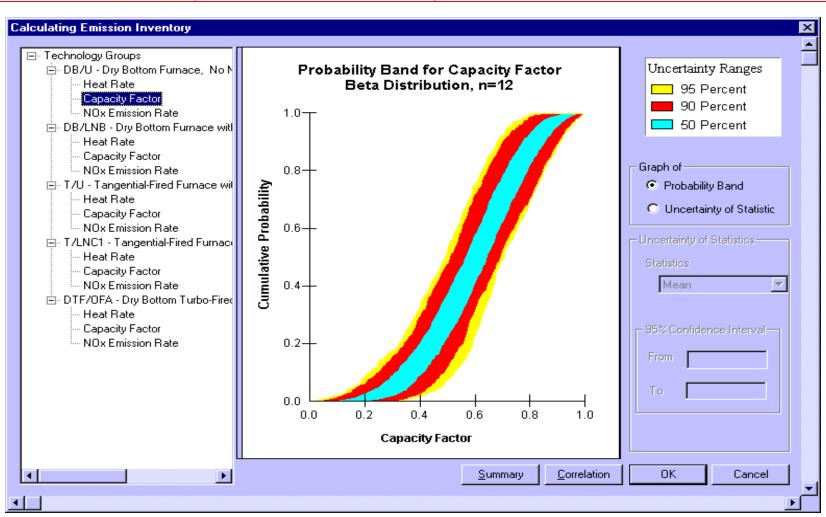




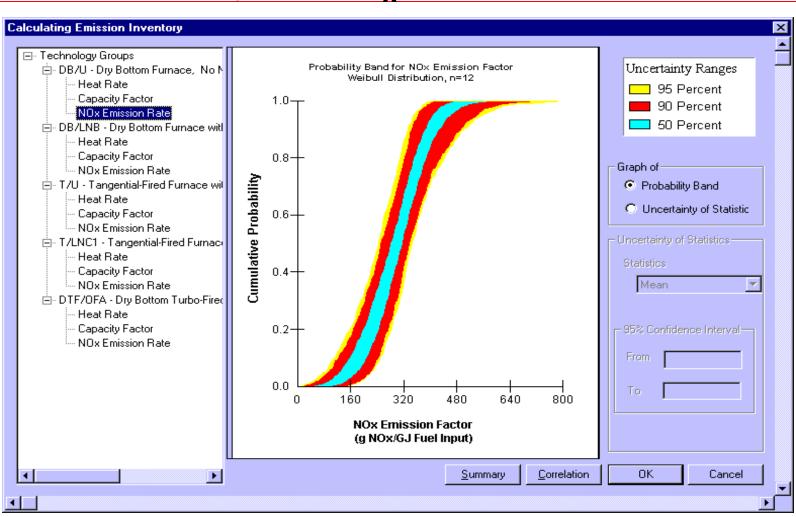
## Characterization of Variability and Uncertainty in Heat Rate: An Example



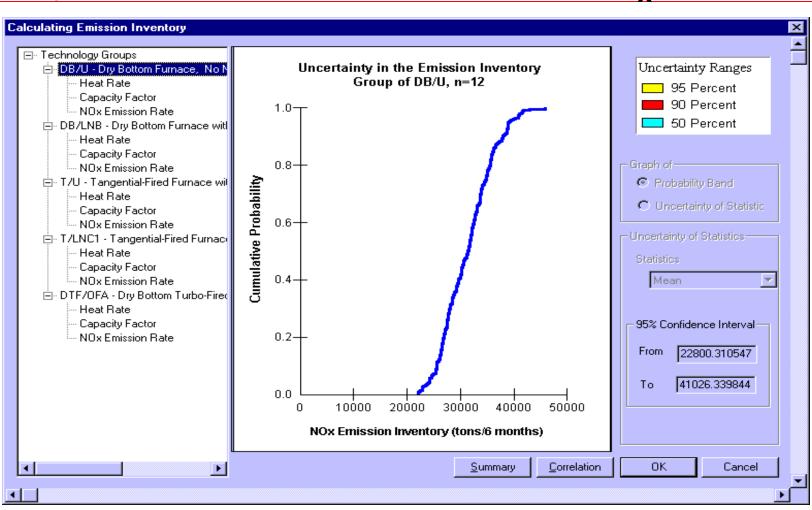
## Characterization of Variability and Uncertainty in Capacity Factor: An Example



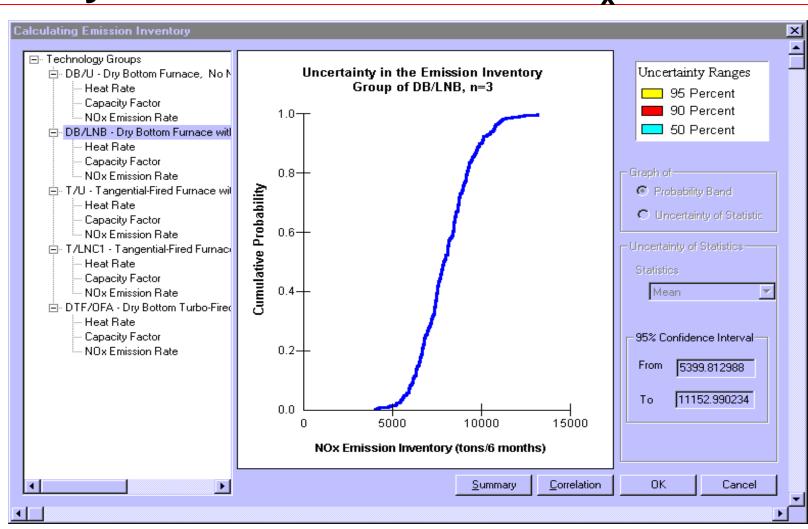
# Characterization of Variability and Uncertainty in NO<sub>x</sub> Emission Factors



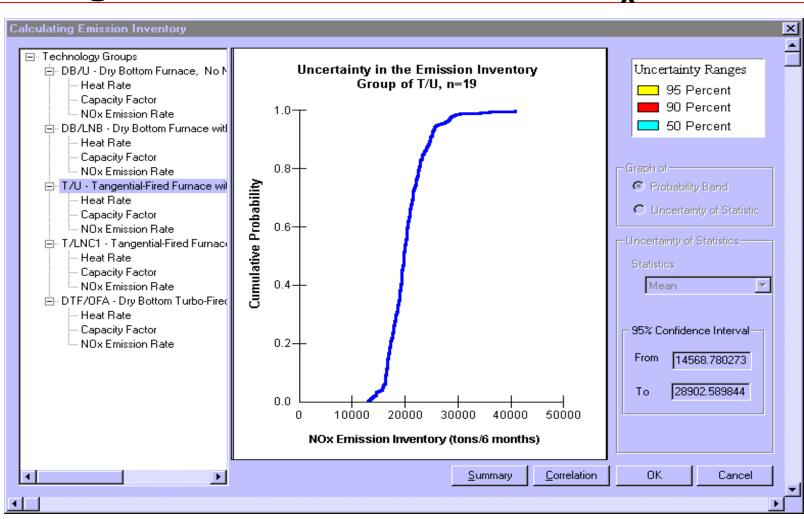
## Uncertainty in Emission Inventory for Dry-Bottom Boilers with No NO<sub>x</sub> Control



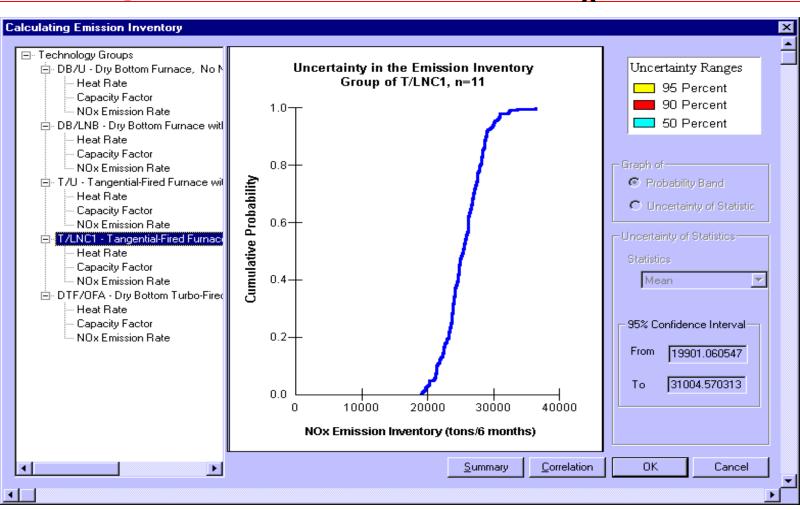
# Uncertainty in Emission Inventory for Dry-Bottom Boilers with NO<sub>x</sub> Control



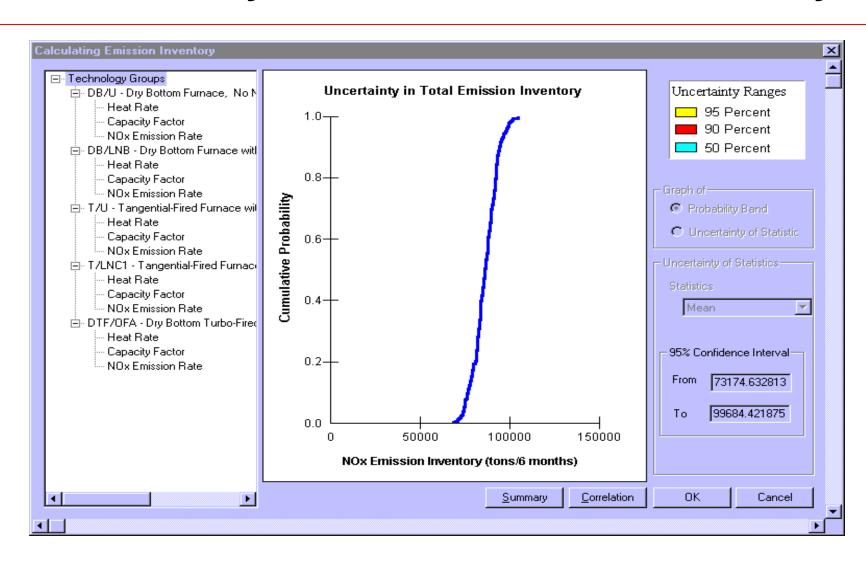
# Uncertainty in Emission Inventory for Tangential Boilers with No NO<sub>x</sub> Control



# Uncertainty in Emission Inventory for Tangential Boilers with NO<sub>x</sub> Control



### **Uncertainty in Total Emission Inventory**

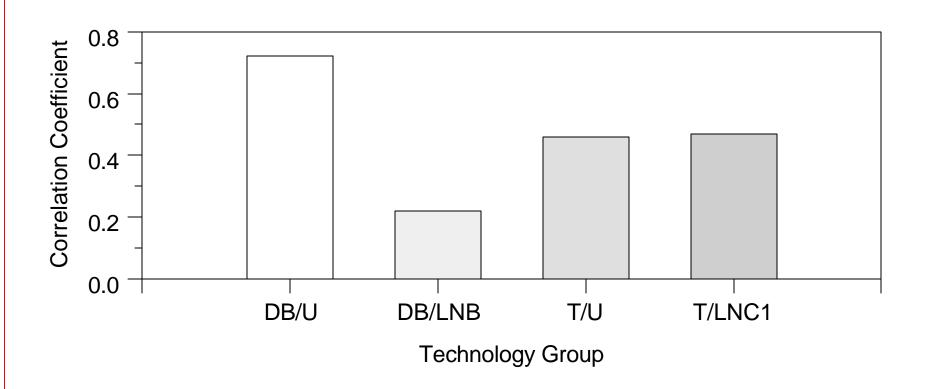


## Summary of Probabilistic Emission Inventory

Technology Group	2.5 <sup>th</sup> Percent	Mean	97.5 <sup>th</sup> Percentile	Random Error (%) <sup>a</sup>	
				Negative	Positive
DB/U	21,700	31,100	40,100	-30	+29
DB/LNB	5,600	8,100	11,400	-31	+39
T/U	15,300	20,400	28,600	-25	+40
T/LNC1	19,800	25,200	31,100	-21	+23
Total	71,800	84,800	99,900	-15	+18

<sup>&</sup>lt;sup>a.</sup> Results shown are the relative uncertainty ranges for a 95 percent probability range, given with respect to the mean value.

### Identification of Key Sources of Uncertainty



### Conclusion

- Demonstrated a general methodological approach for quantifying variability and uncertainty in air pollutant emission inventories
- Developed a prototype software tool to implement the methodology
- Visualization of emission and activity factor databases
- Identification of key sources of uncertainty to help analysts improve the quality of the inventory
- Quantification of uncertainty in 6-month emissions
  - Quality of emission inventory estimates
  - Likelihood of meeting emissions budgets
  - Other decision implications (e.g., trends, air quality modeling)

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For more information:

http://www4.ncsu.edu/~frey/